

0-D integral

1-D integral

2-D integral

3-D integral

Eval f at point 1-var integral

$$f: \mathbb{R}^1 \rightarrow \mathbb{R}$$

$$\xleftarrow{f(x_0)} \xrightarrow{\frac{df}{dx}} \xleftarrow[b]{a} \int f(x) dx$$

$$\mathbf{F}: \mathbb{R}^2 \rightarrow \mathbb{R}^2$$

$$\int_{t_0}^{t_1} \mathbf{F}(\mathbf{r}(t)) \cdot \mathbf{r}'(t) dt$$

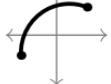
Work

$$\nabla f \text{ (grad)}$$

Eval f at point Line integral

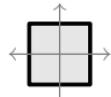
$$f: \mathbb{R}^2 \rightarrow \mathbb{R}$$

$$\xleftarrow{f(x_0, y_0)}$$



$$\int_{t_0}^{t_1} f(\mathbf{r}(t)) |\mathbf{r}'(t)| dt$$

Area integral

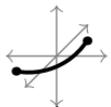


$$\int_{a_1}^{b_1} \int_{a_2}^{b_2} f(x, y) dx dy$$

Eval f at point Line integral

$$f: \mathbb{R}^3 \rightarrow \mathbb{R}$$

$$\xleftarrow{f(x_0, y_0, z_0)}$$



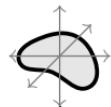
$$\int_{t_0}^{t_1} f(\mathbf{r}(t)) |\mathbf{r}'(t)| dt$$

$$\nabla f \text{ (grad)}$$

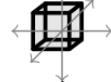
Work

$$\int_{t_0}^{t_1} \mathbf{F}(\mathbf{r}(t)) \cdot \mathbf{r}'(t) dt$$

Surface integral



Volume integral

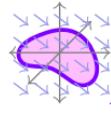


$$\int_{a_1}^{b_1} \int_{a_2}^{b_2} \int_{a_3}^{b_3} f(x, y, z) dx dy dz$$

$$\nabla \cdot \mathbf{F} \text{ (div)}$$

$$\mathbf{F}: \mathbb{R}^3 \rightarrow \mathbb{R}^3$$

Flux



$$\int_{u_0}^{u_1} \int_{v_0}^{v_1} \mathbf{F}(\mathbf{r}(u, v)) \cdot \left(\frac{\partial \mathbf{r}}{\partial u} \times \frac{\partial \mathbf{r}}{\partial v} \right) du dv$$